## \section*{ploring Rules and Patterns} <br> Chapter 15 Exploring Rules and Patterns

 What is the Rule?
## STIEP 1 Completing the Table

What numbers are missing?

| in | 1 | 2 | 3 |  | 5 |  | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| out | 3 | 4 | 5 | 6 |  | 8 |  |



STIP 2 Describing the Rule
What is the rule for the machine? $\qquad$
Explain how you know.
$\qquad$

## STIEP 3 Creating a New Rule

Think of a rule for this machine.

Complete the table.


## (1) School-Home Connection

## Dear Family,

Today we started Chapter 15 in Think Math! In this chapter, I will use patterns to identify rules for rule machines. I will also use rules to explore how to convert different kinds of measurement units. There are NOTES on the Lesson Activity Book pages to explain what I am learning every day.

Here are some activities for us to do together at home. These activities will help me learn to recognize patterns and figure out rules to describe them.

## Love,

## Family Fun

## What's My Number?

Play this game with your child. Your child will also play this game in class.

The first player picks a secret number smaller than 30 .
The second player tries to guess the number. For each guess, the first player responds with "too big," "too small," or "that's right" and records the number in a table like the one shown below.

| Too big | Too small | That's it! |
| :---: | :---: | :---: |
| 25 | 10 | 15 |
| 20 | 13 |  |

When the second player guesses the secret number, players switch roles and play a new game.

## Making Rectangles

Work with your child to practice making rectangular arrays.

You will need grid paper and a number cube.

Take turns tossing the number cube two times to determine the number of rows and the number of columns in a rectangular array. Draw the array on the grid paper.

$\qquad$

## Chapter 15

## Lesson 1

## Identifying Rules

NCTM Standards 1, 2, 6, 7, 8, 9, 10

## What is missing? <br> What is the rule?

I.


| in | 23 | 57 | 54 | 79 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| out | 20 | 54 | 2 |  | 63 | 37 |

The rule is $\qquad$


| in | $A$ | $F$ | $Q$ | $W$ |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| out | C | H | S |  | $V$ | $L$ |

The rule is $\qquad$ .

What is missing?
What is the rule?
3.


| in | 40 |
| :--- | :---: |
| out | 63 |


| 12 |
| :--- |
| 35 |


| 31 | 27 |
| :--- | :--- |
| 54 |  |



The rule is
4. word in


| in | clown | foot | rule | three | plus |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| out | c | f |  |  |  |  |
|  |  |  |  |  |  |  |

The rule is $\qquad$

## Challenge

5. Use the rule machine in Problem 4. What words give was an output?

$\qquad$

## Chapter 15

## Lesson 2 Sorting Rules

NCTM Standards 1, 2, 6, 7, 8, 9, 10

## What is missing?

I.

2.


| in | 31 | 78 | 3 |
| :--- | :---: | :---: | :---: |
| out | yes | no | yes |



## What is missing?

| 6 | no |
| :--- | :--- |


4.


| in | out |
| :---: | :---: |
| 6 in. | no |


| 14 in. | yes |
| :---: | :---: | 12 inches $\square 1$ foot


| 9 in. | no |
| :--- | :--- |

II in.

24 in.


Challenge
5. What is missing?

What is the rule?


The rule is $\qquad$ .
$\qquad$

## Chapter 15

## Lesson 3 Undoing Rules

## Write the missing numbers. What is the rule?

I.


| in | 20 | 15 | 40 | 33 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| out | 30 | 25 |  |  |  | 60 |

The rule is $\qquad$
2.


| in | 67 | 40 | 25 | 80 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| out | 57 | 30 |  |  | 50 | 31 |

The rule is $\qquad$ .
3. What do you notice about the rules for Problems I and 2?

Write the missing numbers. Use a calculator if you like.
What is the rule?
4.


| in | 2 | 10 | 9 |
| :--- | :---: | :---: | :---: |
| out | 20 | 28 |  |



The rule is
5.


| in | $12: 00$ | $1: 30$ |
| :--- | :--- | :--- |
| out | $12: 30$ | $2: 00$ |



The rule is $\qquad$

## Challenge

6. Write rules to undo the rules in

Problem 4 and Problem 5.
Problem 4 $\qquad$
Problem 5 $\qquad$
$\qquad$

## Chapter 15

## Lesson 4

## Rules with More Than One Input <br> NCTM Standards 1, 2, 6, 7, 8, 9, 10

## What is missing?

I.


| in | 6 | 10 |
| :--- | :---: | :---: |
| in | 2 | 8 |
| out | 4 | 2 |


| 15 |
| :---: |
| 5 |
| 10 |


| 20 |
| :---: |
| 15 |
|  |


| 17 | 48 |
| :---: | :---: |
|  |  |
| 13 | 18 |

2. 



Write the missing numbers.
3.


| in | 1 |
| :--- | :---: |
| in | 3 |
| out | 2 |


| 5 |
| :---: |
| 7 |
| 6 |


|  | 33 |
| :--- | :--- |
| 51 | 35 |
|  |  |


| 67 |  |
| :---: | :---: |
| 69 |  |
|  | 55 |

4. 

| in | 5 | 14 | 79 | 40 | 25 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| in in | 8 | 23 | 76 | 12 | 15 | 6 |
| in | 20 | 6 | 70 | 18 | 5 |  |
| out | 20 | 23 | 79 |  |  | 10 |

## Challenge

5. If I know an output for Problem 3, then I know both inputs because
$\qquad$

## Chapter 15

## Lesson 5

## Conversion Rules

NCTM Standards 1, 2, 3, 4, 6, 7, 8, 9, 10

## Write the missing numbers.

I.


| Number <br> of pints |
| :--- |
| Number <br> of cups |


2.



Write the missing numbers. Use a calculator if you like.
3.

| Number of <br> quarters | 1 | 2 | 3 | 6 | 10 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> nickels | 5 | 10 | 15 |  |  |  |

4. 

| Number of <br> gallons |
| :--- |
| Number of <br> quarts |


| 1 |
| :---: |
| 4 |


| 3 |
| :---: |
| 12 |


| 10 | 2 |
| :---: | :---: |
| 40 |  |


| 5 |
| :--- |
|  |


| 6 |  |
| :---: | :---: |
|  | 16 |

## Challenge

5. 

| Number of <br> yards | 1 | 2 | 3 | 5 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of <br> feet | 3 | 6 | 9 |  |  |

6. What is the rule?
7. Explain how you found the missing numbers.
$\qquad$
$\qquad$
$\qquad$

## Chapter 15

## Lesson 6

## Skip-Counting with Money

NCTM Standards 1, 2, 4, 6, 7, 8, 9, 10


Use the prices above. How much will the blocks cost?

7.

$\qquad$
$\not \subset$
8.


## Use the Pattern Block Prices from page 317.

9. Kyra bought 4 blocks.

They cost 20¢.
What color blocks did Kyra buy?

IO. Jamal bought these blocks. He paid with a dollar bill.


How much did the blocks cost? $\qquad$
$\phi$
How much was his change? $\qquad$
II. Sue bought twice as many She spent 16¢.
What did she buy?

12. Dex bought one kind of block. He paid 18¢.
What color could his blocks be?
or

## Problem Solving

13. Tamara spent I24. She got 3 blocks.

They were not all the same.
What color could her blocks be?
and $\qquad$
$\qquad$

Chapter 15

## Lesson 7

## Creating Figures and Patterns

NCTM Standards 1, 2, 6, 7, 8, 9, 10
Complete each table.
I. I am making fish.


| Number of fish | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Cost of | $3 \phi$ | $6 \phi$ | $9 \phi$ |  |  |  |
| Cost of | $2 \phi$ | $4 \phi$ | $6 \%$ |  |  |  |
| Total cost | $5 \phi$ | 6 |  |  |  |  |

2. I am making computers.

| Number of <br> computers | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Cost of | $4 \varnothing$ |  |  |  |  |  |
| Cost of | $1 \varnothing$ |  |  |  |  |  |
| Total cost | $5 \varnothing$ |  |  |  |  |  |

Complete each table.
3. I am making fancy hexagons.

| Number of hexagons | I | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cost of |  |  |  |  |  | $\mid 6$ |
| Cost of |  |  |  | - |  |  |
| Cost of |  |  | \% |  |  |  |
| Total cost |  |  |  |  |  |  |

4. I am making houses.

| Number of <br> houses | 1 | 2 | 3 | 5 | 7 | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Cost of | 56 |  |  |  |  |  |
| Cost of | 46 |  |  |  |  |  |
| Total cost | 96 |  |  |  |  |  |

$\qquad$

## Chapter 15

## Lesson :

## Patterns with Skip-Counting <br> NCTM Standards 1, 2, 6, 7, 8, 9, 10

I. Skip-count on the grid below. Mark jumps of 4 and 6 .


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |

2. Skip-count on the grid below. Mark jumps of 8 with an Mark jumps of 7 with an O .

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 6 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |

3. Look at the grid in Problem 2.

Where do the jumps meet?
Find 8 .

## Problem Solving

4. What numbers are missing?

I start at 0 .
I make $\qquad$ ___ jumps of 7
to get to $\qquad$ .
$\qquad$
Chapter 15 Lesson ${ }^{\circ}$

## Relating One-Color Trains

NCTM Standards 1, 2, 6, 7, 8, 9, 10

## Write the missing numbers.



## Write the missing numbers.

| 6. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | , |  |  |  |  |  | is as long as |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | is as | 崖 |  |  |  |  |  |
|  |  | 2 |  |  |  |  |  | are as | long as |  |  |  |  |  |
|  |  |  |  |  |  |  |  | areas | , as |  |  |  |  |  |
|  |  |  |  |  |  |  |  | are as | long as | 6 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 7. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 3 |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | are | as | long |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | or |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

8. What pattern do you notice in Problem 7?

## Challenge

9. Build matching trains. Write the missing numbers.

|  |  |  | 6 | 9 | 12 |  | 30 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 2 |  |  |  | 12 |  | 10 |
|  |  |  |  |  |  |  |  |

$\qquad$

## Chapter 15

## Lesson 10

# Problem Solving Strategy Work Backward <br> NCTM Standards 1, 2, 6, 7, 8, 9, 10 

I. Joe had some money.

He got 27¢ more.
He spent I5¢.
Now he has 27c.
How much money did Joe start with?
$\qquad$
2. Wilbur collects stuffed toy bears.

He got 2 new bears every year.
When he was 10 years old, he had 20 bears.
How many bears did he have
when he was 4 years old?
$\qquad$ bears
3. Paula makes quilts.

Each year she makes I less quilt than she did the previous year.
This year she made 3 quilts.
How many quilts did she make 4 years ago?
quilts

## Problem Solving Test Prep

I. Lin puts I2 red and white flowers in a vase.
There are 4 more red flowers than white flowers.
How many red flowers are there?
(A) 4
(C) 8
(B) 6
(D) 12
2. Ethan makes items for the craft fair. He makes 3 bookmarks and 4 cards each day. How many items will he make in 3 days?
(A) 3
(C) 7
(B) 4
(D) 21

## Show What You Know

3. Hannah has I2 square tiles. How many different rectangles can she make?
$\qquad$ rectangles
Use words, numbers, or pictures to explain.
4. Kate skip-counts by twos.

Dan skip-counts by threes.
They both start at 0 .
What is the first number both Kate and Dan will say?

Explain how you found the answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Chapter 15 <br> Review/Assessment

## Write the missing numbers. <br> What is the rule? <br> Lessons 1, 2, 3, and 4

I.


| in | 4 | 12 | 10 |  | 2 | 21 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| out | 8 | 16 | 14 | 5 |  |  |

The rule is $\qquad$

Write the missing numbers.
Lesson 5
2.

| Number of <br> quarts | 1 | 2 | 3 | 5 |  | 7 |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> cups | 4 | 8 | 12 |  | 40 |  | 16 |

## What is the cost?

3. One of these costs $\qquad$ ¢.
4. Three of these cost $\qquad$ ¢.


Skip-count on the grid below. Lesson 8
5. Mark jumps of 3 with an .

Mark jumps of 4 with an $O$.

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |

6. Where do the jumps above meet?

Find $\bigotimes$.
Lesson 8

Write the missing number. Lesson9


## Problem Solving ${ }_{\text {Lesson } 10}$

8. Carla had some coins.

She found $23 ¢$ more.
Then she spent I2¢.
Now Carla has 264.
How much did Carla start with?

